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This guide details the highlights of the process in making your very own suspension bridge out of simple, cheap materials. To make the suspension bridge in the sample, the builder/creator (jamesabt007) used the following materials and tools:

Materials

- Cardboard
- Popsicle Sticks ( 24 for a bridge with 1 deck, 36 for 2 decks, etc.)
- String
- Scotch Tape

Tools

- Large Nail, Hobby Knife or Box cutter
- Scissors
- Ruler
- Pen/Pencil
- Sand Paper
- Elmer's Glue or Craft Glue

First, We'll Make the Pylons
For each pylon (Picture 1-Upper Left), you will need 12 Popsicle sticks. Make two I beams, two L beams (Picture 2-Upper Right). And then combine them with each other and two separate Popsicle sticks.

Use the following series of images for reference as you complete the previous steps and make a pylon.

Make at least three pylons.


Image Notes

1. Your goal.


Image Notes

1. Your second goal


Image Notes

1. This sidewayness really bothers me, sorry if it also bother you.


Image Notes

1. Your end result.


Image Notes

1. Your I-beam, sort of looks like a hot-dog if you ask me.



## Making the $\operatorname{Deck}(s)$

To make the deck for the bridge, start out with a relatively medium sized cardboard. The piece in the following images was large enough to fit two decks.

Depending on how many decks you want your bridge to have, you can make more or less.

Measure out the deck, mark the holes from the
 intersections to where
you will punch holes for the suspension cables to go through, cut the piece.
Tip: if you are using a knife to punch the holes for students, be sure to have students clean them by either making them larger than needed or by forcing the material aside such that there is a distinct hole with a pen or pencil or large nail. This is to ensure that the string can easily be threaded through the holes and will make the process a lot easier to make the decks.


## String

Your lengths of string can vary depending on the distance from pylon to pylon, your total span of the bridge, and your height you want the decks to be above the ground. Use a ruler and explore with different lengths to see which bridge looks nicer or more realistic.

## Stringing the deck(s)

This part of the process is placing the string you determined from the previous step into the holes of the deck. There are many ways to do this step.

Just remember that if you have 5 total suspenders on each side of the deck, you'll need to make the 4 holes on each corner of

## Tip!

If you hold a piece of string from both ends and let it hang downwards with nothing attached to it, it will create the shape that your finished suspension bridge's cable should have- you can then copy this shape to a piece of paper or cardboard and use it to figure out how long the suspender cables should be. This shape is also the shape of an ideal arch bridge upside down. the deck have longer loops than the one in the middle since the cable droops slightly, like the curve of a parabola with a positive a coefficient ( $y=a \times 2+b x+c$ ).


Image Notes

1. Your goal. Once done, do for all 4 other holes.
2. You want to create a loop here on the topside so that the suspender can be strung through it later.

Top of Bridge Deck- a look into how to start the stringing process.


Bottom of Bridge Deck- a look into how to start the stringing process.

Bringing it
together
These are a
few images and close ups of a completed model.
Remember that this is a very open ended project with no real set guidelines on the lengths and distances just like suspension bridges in real life.


There are many ways this bridge can be built!


## 

## Akashi Kaiyko Bridge: The Longest Bridge in the World (so Far)

Bridges are the lifeline of Japan. Since the 1930s, the island nation has dreamt of linking its many parts as a whole. But WWII diverted the incredible resources needed to accomplish this, and only since 1960 has the dream moved again, slowly, toward reality. The final step in this massive undertaking was the Akashi-Kaikyo Bridge, currently the longest single-span suspension bridge in the world. This marvel of architectonics stands as a testament to the genius of Asian engineering and, judged in a context that perhaps the Japanese understand best, as the most beautiful bridge in the world.

In 1998, Japanese engineers stretched the limits of bridge engineering with the completion of the Akashi Kaikyo Bridge. Currently the longest spanning suspension bridge in the world, the Akashi Kaiyko Bridge stretches 12,828 feet across the Akashi Strait to link the city of Kobe with Awaji-shima Island. It would take four Brooklyn Bridges to span the same distance! The Akashi Kaikyo Bridge isn't just long -- it's also extremely tall. Its two towers, at 928 feet, soar higher than any other bridge towers in the world.


The Akashi Strait is a busy shipping port, so engineers had to design a bridge that would not block shipping traffic. They also had to consider the weather. Japan experiences some of the worst weather on the planet. Gale winds whip through the Strait. Rain pours down at a rate of 57 inches per year. Hurricanes, tsunamis, and earthquakes rattle and thrash the island almost annually.

How did the Japanese engineers get around these problems? They supported their bridge with a truss, or complex network of triangular braces, beneath the roadway. The open network of triangles makes the bridge very rigid, but it also allows the wind to blow right through the structure. In addition, engineers placed 20 tuned mass dampers (TMDs) in each tower. The TMDs swing in the opposite direction of the wind sway. So when the wind blows the bridge in one direction, the TMDs
sway in the opposite direction, effectively "balancing" the bridge and canceling out the sway. With this design, the Akashi Kaikyo can handle 180-mile-per-hour winds, and it can withstand an earthquake with a magnitude of up to 8.5 on the Richter scale!

Here's how this bridge stacks up against some of the longest-spanning bridges in the world. (Total length, in feet)


## Akashi Kaikyo Bridge 12,828'

## Fast Facts:

- The bridge is so long, it would take eight Sears Towers laid end to end to span the same distance.
- The length of the cables used in the bridge totals 300,000 kilometers. That's enough to circle the earth 7.5 times!
- The bridge was originally designed to be 12,825 feet. But on January 17,1995 , the Great Hanshin Earthquake stretched the bridge an additional three feet.
- The bridge holds three records: it is the longest, tallest, and most expensive suspension bridge ever built.

Vital Statistics:
Location: Kobe and Awaji-shima, Japan
Completion Date: 1998
Cost: $\$ 4.3$ billion
Length: 12,828 feet
Type: Suspension
Purpose: Roadway
Materials: Steel
Longest Single Span: 6,527 feet
Engineer(s): Honshu-Shikoku Bridge Authority


Option: Watch selected clips from Modern Marvels - The World's Longest Bridge (by the History Channel) if available and/or clips from The Longest Suspension Bridge in The World by Big, Bigger, Biggest.

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When engineers are building a new road they try to pick a route with the fewest number of huge obstacles. Sometimes such a path is impossible to find, especially if a long river, large lake, or deep valley is in the region. When this problem occurs, civil engineers must find a way to safely cross the obstacle according to specifications provided by the town or state. Sometimes the best solution is a tunnel. Sometimes the best solution is a bridge.

Since ancient times, engineers have designed three major types of bridges to withstand all forces of nature. The main three are arch bridges, beam bridges, and suspension bridges (each with variations on the theme). All three have some similar features. Each has a deck (the horizontal surface you drive on) supported by piers (the vertical parts). The span is the distance between the piers. Abutments support the bridge on either side of the span and connect to the ground on either side. The type of bridge selected for a site will depend on the distance the bridge needs to cover, how much weight the bridge must support, and the natural factors (e.g., wind, earthquakes) the bridge must survive.

## 



An arch bridge has a deck supported by an arch underneath. The arch is built from either side with a keystone placed at the center of the arch. The weight of the bridge is thrusted into the abutments at either side. The Romans were famous for creating bridges using this design. The earliest known arch bridges were built by the Greeks and include the Arkadiko Bridge. Some examples of their work still stand today. These bridges are good for shorter spans.

A beam bridge is a horizontal deck surface supported by piers or supports on either side of the stream. Weight on top of the beam pushes straight down on the piers at either end of the bridge. The earliest beam bridges were simple logs that sat across streams and similar simple structures. In modern times, beam bridges are large box steel girder bridges.

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One important example of a beam bridge is a truss bridge (which are often put into their own category of bridges as well). Wooden truss bridges were used as early as the 1700s, but the first metal one was completed in 1841. They are very strong and have been used for railroad bridges mainly because of the heavy loads they can support. A truss, a rigid support structure
 that is made up of interlocking triangles, holds up the roadbed and is set between two piers. The triangle is used because it is the only shape that is inherently rigid.

Truss bridges are composed of connected elements. They have a solid deck and a lattice of pin-jointed girders for the sides. A truss is a structure made up of triangles. The triangular shape makes a truss very strong to support its weight. Historically, these trusses were made from wood and, to prevent decay, the bridge would be covered. Now, trusses are made of steel to withstand the weather.

## Pros and Cons of Truss Bridges

Pros: Very strong; frequently used as a draw bridge
Cons: Difficult to construct; high maintenance; difficult to widen if necessary; generally not considered attractive.

Compression and Tension
Compression: As traffic
 pushes down on the roadway, compression acts on the upper horizontal members of the truss structure.

Tension: Tension acts on the bottom horizontal members of the truss structure. The forces of tension and compression are shared among the angled members.

Cantilever: Cantilever bridges are built using cantilevers - horizontal beams that are supported on only one end. Most cantilever bridges use two cantilever arms extending from opposite sides of the obstacle to be crossed, meeting at the center.

## Truss Bridge Challenge

In this activity from TryEngineering.org (Developed by IEEE as part of TryEngineering), students will explore why trusses are used in bridges to add strength and stability. Truss bridges are constructed by connecting a framework of triangles. Trusses are a key engineering concept because they do not change when force is applied. The triangular shapes help to spread the force evenly around the three sides.

Introduce the activity by asking students if they think a triangle is sturdier or stronger than a square. Many students may initially predict that a square will be sturdier since it has more sides. Provide each student with 2 plastic drinking straws. Instruct the students to create an equilateral triangle shape with one and a square shape with the other. Use tape to secure the two ends and complete the shape. Allow students to apply force to one corner of the square and note how the shape changes into a diamond shape. Apply force to one corner of the triangle and discuss how the shape doesn't change as easily because the three sides distribute the force more evenly.

Divide the students into small groups of 3 or 4. Provide each group with the following materials:

- Graph paper to design their bridge
- Craft sticks (100 sticks per group)
- Heavy-duty scissors or wire cutters for cutting the craft sticks
- Elmer's Glue-All or Craft Glue
- Binder clips
- Truss Bridge Challenge (handout)

Show the students a sample bridge or pictures of truss bridges. Point out that the sides of the bridge are made up of many triangles that add stability. Instruct the students to follow the instructions on the handout to construct their own truss bridge. Remind them that engineers must stay within a budget when building bridges.

## Truss Bridge Challenge!

The Problem: The National Railroad Company has added a new fleet of trains to transport goods across the country. A narrow river runs through a deep valley in one section of the railroad plan. A new bridge must be constructed to accommodate the railroad addition. The bridge must be stable enough to keep the train level as it crosses the valley.

The Challenge: A representative from the city has contacted you to design a model of a truss bridge that will be stable enough to keep the train level as it crosses the valley.

The Materials: You can only use craft sticks and Elmer's Glue-All to construct the bridge. You may use binder clips to hold the craft sticks in place until the glue dries, but they must not be included in the final bridge design.

The Cost: Your truss bridge must be cost-efficient to build. You have a budget of $\$ 100,000$ to construct it. Using the cost of materials below, calculate the cost of your bridge.

Beams (craft sticks) = \$1000 each
Iron joints (glue) = \$5000/bottle

## Brainstorm, Design and Build!

What design do you think would be the best for this challenge? Sketch your bridge design on a piece of paper and identify some ways that you might make it stable enough and strong enough to support the train while staying within your budget. Build your model and test it to see if you will get the job!

With a few craft sticks, some Elmer's Glue-All, and a lot of patience you can build an amazing truss bridge. Here are some tips to get you started.

1. Begin by building the side trusses. Start by building the top, bottom and sides in the shape of an isosceles trapezoid. Use four craft sticks on the bottom, three on the top and one on each side. Make sure the top and bottom are straight, glue them side pieces in place, and let them dry.

2. Next, add a stick to each joint to create the trusses inside.

3. Lean the side pieces against thick heavy books so that you can add the top of the bridge. Construct the top of the bridge by connecting the sides with a craft stick at each joint.
4. Decide the best way to construct the top and the bottom of the bridge and attach the sides. Remember, you must stay under budget and your bridge must be sturdy enough to support the train and keep it level.



VAULTED PARALLEL CHORD


FLAT VAULT


BARREL VAULT


POLYNESIAN


GAMBREL


ROOM-IN-ATTIC



CANTILEVERED MANSARD WIPARAPETS


MULTI-PIECE



Tip：There is no specific reason that we have to only consider＂upward options＂．We could try something like this：

or even this：


Or a design of our own invention！

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## Addition and Subtraction

Fact families help students to see how addition and subtraction are related to one another. (For example: If $6+4=10$, then $4+6=10$. Furthermore, if $10-6=4$, then $10-$ 4=6.) Show children a triangle of related numbers, e.g. 1275

Teams then race to be the first to write the 2 addition facts and 2 subtraction facts in the family, i.e. $7+5=12,5+7=12,12-5=7,12-7=5$.


Fact Families are sets of three numbers that can be divided or multiplied together and they help develop the understanding of the relationship between multiplication and division.

Show students a triangle of related numbers, e.g. 2438
Children then race to be the first to write the 2 multiplication facts and 2 division facts in the family, i.e. $3 \times 8=24,8 \times 3=24,24 \div 3=8,24 \div 8=3$.

Resource: The print-outs at this link from Donna Young are triangle flash cards. These cards are smaller than commercial cards. They measure about 4 inches along each of the sides. There are 9 flash cards on each of the print-outs with the exception of the $3 \times 3=9$ card, which has only 6 flash cards.

No math fact is repeated, so in order to get all the math facts from either the addition/subtraction group or the multiplication/division group, you'll need to print all the cards.

The addition and subtraction cards cover the facts from $0+1=1$ to $9+9=18$ and the multiplication and division cards cover the facts from $1 \times 1$ to $12 \times 12$. Use the blank cards if you want to make custom cards.


Tri-Ominoes Multiplication \& Subtraction Variations:
Preparation:
You need to print the sets of tri-ominoes with each page of each set printed in a different colors on cardstock and then cut them out
along the dotted lines. For multiplication you will have 20 in each color. One set have two numbers on the sides and the other set have one number. There are three sets of subtraction cards.

How to play:

1. Work in groups of two, three or four. Shuffle and share out the forty tri-ominoes.
2. Throw a die to decide who should start.
3. The first player puts a tri-omino on the table.
4. The second player must put a different colored tri-omino alongside so that the product of the two numbers is equal to the single number.
5. If a player cannot place a tri-omino then they miss a turn.
6. The winner is the player to use up all their tri-ominoes

## Sample Game:

First move

$6=2 \times 3$
Third move


$$
9=3 \times 3
$$

Tri-Ominoes Multiplication First Set he Gap: Woalt 4


Tri-Ominoes Multiplication Second Set the Gap: Weel 4


Tri-Ominoes Subtraction Variation First Set ${ }_{g}$ the Gaps Wale 4



bonus plus the total
deduct these points from their score. WINNING A ROUND: The first player to play all of his Tri-Ominos wins the round and receives a 25 point
 deduction is made, the scorekeeper adds the total sum of points from the matching Tri-Omino to your score.




 |  | 3 |
| :--- | :--- |

## $5+4+3=12$ points

:2duivx
Tri-Omino starts. This player scores the total of the numbers on that Tri-Omino, but does not score any
bonus points. If no player has a Tri-Omino with three of the same number on it, the player with the highest total on one player chooses to start with the three Os to score the additional bonus points, he must show the other play-
ers the Tri-Omino with the same highest number on it. The player that has the starting Tri-Omino and the three $O$ s has the option of playing either one. If this
 :2duives receives the total of the three numbers on the Tri-Omino plus a 10 point bonus. If three 0 s start, there is a
30 point bonus, plus the normal 10 point bonus.
 Players place the tiles on the rack with the numbers facing them. Do not let the other players see your tiles. 9 each
7 each
 player. As each play is made, the scorekeeper will add or subtract points in the proper column.
Each player takes the required number of Tri-Ominos as follows: SET UP: Place the Tri-Ominos face down and mix them. On a piece of paper, write down the name of each OBJECT: Be the first player to score 400 points. Each game consists of several rounds.
CONTENTS: 56 Tri-Omino tiles, 4 Racks. For 2 to 4 players
Ages 8 to adult
OBJECT: Be the

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The following are selected from the comprehensive list of the math skills students learn in each grade． Remember，these skills build on each other．They are assuming that students have mastered all the ones in the previous grades．

The skills are organized into categories：As you read（and complete）the activities in the plan，keep in mind the specifics skills your students need to practice and master in the different grade levels you work with．Use their needs to guide your approach in how you＇ll modify and present the activities and what specific tasks you will have the students do．

## 脗嵒

Adding
－I． 1 Addition with pictures $\sim$ sums up to 5
－I． 2 Add two numbers $\sim$ sums up to 5
－I． 3 Addition sentences $\sim$ sums up to 5
－I． 4 Ways to make a number～sums up to 5
－I． 6 Addition with pictures $\sim$ sums up to 10
－I． 7 Add two numbers～sums up to 10
－I． 8 Addition sentences $\sim$ sums up to 10
－I． 9 Ways to make a number～sums up to 10
－I． 10 Addition word problems $\sim$ sums up to 10
Subtracting
－J． 1 Subtract with pictures～numbers up to 5
－J． 2 Subtraction～numbers up to 5
－J． 3 Subtraction sentences $\sim$ numbers up to 5
－J． 5 Subtract with pictures～numbers up to 10
－J． 6 Subtraction～numbers up to 9
－J． 7 Subtraction sentences $\sim$ numbers up to 10 Skip～counting
－F． 1 Skip～count by twos
－F． 2 Skip～count by fives
－F． 3 Skip～count by tens
－F． 4 Skip～count by twos，fives，and tens
Positions
－K． 1 Inside and outside
－K． 2 Left，middle，and right
－K． 3 Top，middle，and bottom
－K． 4 Above and below

異
Addition
－B． 1 Addition with pictures～sums to 10
－B． 5 Ways to make a number using addition
－B． 6 Ways to make a number～addition sentences
－B． 7 Adding zero

- B. 8 Adding doubles
- B. 9 Addition facts $\sim$ sums to 10
- B. 10 Addition facts ~ sums to 18
- B. 11 Addition word problems $\sim$ sums to 18
- B. 12 Complete the addition sentence
- B. 13 Adding three numbers
- B. 16 Addition facts $\sim$ sums to 20
- B. 17 Add tens
- B. 19 Add a one -digit number to a two digit number $\sim$ without regrouping
- B. 20 Regrouping tens and ones
- B. 22 Add a one $\sim$ digit number to a two $\sim$ digit number $\sim$ with regrouping Subtraction
- D. 1 Subtraction with pictures ~ numbers up to 10
- D. 2 Subtraction sentences ~ numbers up to 10
- D. 5 Ways to make a number using subtraction
- D. 7 Ways to subtract from a number ~ subtraction sentences
- D. 8 Subtracting zero and all
- D. 9 Subtracting doubles
- D. 10 Subtraction facts ~ numbers up to 10
- D. 11 Subtraction facts ~ numbers up to 18
- D. 16 Subtract tens
- D. 17 Subtract one -digit numbers from two digit numbers Counting and number patterns
- A. 15 Skip counting patterns $\sim$ with tables
- A. 16 Sequences $\sim$ count up and down by $1,2,3,5$, and 10

等
Addition ~ one digit

- E. 1 Review ~ add one $-d i g i t$ numbers ~ sums to 10
- E. 2 Review ~ ways to make a number ~ sums to 10
- E. 3 Review ~ writing addition sentences $\sim$ sums to 10
- E. 4 Add one digit numbers
- E. 5 Addition with pictures ~ sums to 20
- E. 6 Write addition sentences to describe pictures ~ sums to 20
- E. 7 Addition input/output tables ~ sums to 20
- E. 8 Add zero
- E. 9 Addition word problems ~ one digit
- E. 10 Complete the addition sentence $\sim$ one digit
- E. 11 Write the addition sentence ~ one digit
- E. 12 Balance addition equations ~ one digit
- E. 13 Add three or more one-digit numbers

Subtraction ~ one digit

- F. 1 Review ~ subtract one digit numbers ~up to 10
－F． 2 Review～ways to subtract～up to 10
－F． 4 Subtract a one $\sim$ digit number from a two digit number up to 18
－F． 5 Subtraction with pictures
－F． 8 Subtract zero／all
－F． 12 Balance subtraction equations $\sim$ up to 18
Subtraction～two digits
－H． 1 Subtract multiples of 10
－H． 2 Subtract a one $\sim$ digit number from a two digit number $\sim$ without regrouping
－H． 3 Subtract a one～digit number from a two digit number～with regrouping
－H． 4 Subtract two two $\sim$ digit numbers $\sim$ without regrouping
－H． 5 Subtract two two $\sim$ digit numbers～with regrouping
－H． 8 Ways to make a number using subtraction
－H． 12 Balance subtraction equations $\sim$ up to two digits
Subtraction～three digits
－J． 1 Subtract multiples of 100
－J． 2 Subtract three digit numbers
－J． 7 Balance subtraction equations～up to three digits
Multiplication
－W． 1 Multiplication sentences
－W． 2 Multiplication tables up to 5
－W． 3 Multiplication tables up to 10
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Addition
－C． 1 Add two numbers up to three digits
－C． 2 Addition input／output tables～up to three digits
－C． 4 Complete the addition sentence $\sim u p$ to three digits
－C． 5 Balance addition equations～up to three digits
－C． 6 Add three or more numbers up to three digits each
－C． 8 Addition patterns over increasing place values
－C． 9 Add two numbers with four or more digits
－C． 12 Complete the addition sentence $\sim$ four or more digits
－C． 13 Balance equations $\sim$ four or more digits
－C． 14 Add three or more numbers with four or more digits
Subtraction
－D． 1 Subtract numbers up to three digits
－D． 4 Subtraction patterns over increasing place values
－D． 5 Balance subtraction equations～up to three digits
－D． 7 Subtract numbers with four or more digits
Multiplication
－E． 1 Multiplication sentences
－E． 2 Multiplication～facts to 12
－E． 4 Missing factors～facts to 12
－E． 6 Squares up to 20
－E． 7 Multiplication patterns over increasing place values
－E． 8 Multiply by a multiple of ten
－E． 9 Multiply numbers ending in zeroes
－E． 10 Multiply a one $\sim$ digit number by a larger number
－E． 12 Multiply three or more numbers
罍
Addition
－B． 1 Add numbers up to millions
－B． 3 Addition：fill in the missing digits
－B． 4 Properties of addition
－B． 5 Add 3 or more numbers up to millions
－B． 6 Addition patterns over increasing place values
－B． 7 Choose numbers with a particular sum
－B． 8 Estimate sums
－B． 9 Estimate sums：word problems
Subtraction
－C． 1 Subtract numbers up to millions
－C． 3 Subtraction：fill in the missing digits
－C． 4 Subtraction patterns over increasing place values
－C． 5 Choose numbers with a particular difference
－C． 6 Estimate differences
Multiplication
－D． 1 Multiplication facts to 12
－D． 2 Missing factors $\sim$ facts to 12
－D． 3 Choose the multiples of a given number up to 12
－D． 4 Identify factors
－D． 5 Multiply $1 \sim$ digit numbers by larger numbers
－D． 7 Properties of multiplication
－D． 8 Estimate products
－D． 10 Multiply a 2～digit number by a 2～digit number：complete the missing steps
－D． 11 Multiply a 2～digit number by a 2～digit number
－D． 13 Choose numbers with a particular product
－D． 15 Multiply a 2～digit number by a larger number
－D． 17 Multiply numbers ending in zeroes
－D． 19 Multiply 3 numbers up to 2 digits each

Addition and subtraction
－D． 1 Add and subtract whole numbers up to billions
－D． 5 Complete addition and subtraction sentences
－D． 6 Fill in the missing digits
－D． 7 Choose numbers with a particular sum or difference
－D． 8 Properties of addition
－D． 10 Estimate sums and differences of whole numbers
－D． 11 Estimate sums and differences：word problems
Multiplication
－F． 1 Multiply by 1～digit numbers
－F． 3 Multiplication patterns over increasing place values
－F． 4 Multiply numbers ending in zeroes
－F． 6 Properties of multiplication
－F． 7 Choose numbers with a particular product
－F． 8 Estimate products
－F． 10 Multiply by 2～digit numbers：complete the missing steps
－F． 11 Multiply a 2～digit number by a 2～digit number
－F． 12 Multiply a 2～digit number by a larger number
－F． 14 Multiply three or more numbers up to 2 digits each
－F． 15 Multiply by 3～digit numbers
－F． 16 Multiply three numbers up to 3 digits each
晋
Add and subtract integers
－I． 1 Review～add and subtract whole numbers
－I． 3 Properties of addition
－I． 4 Integer addition and subtraction rules
－I． 7 Subtract integers～using counters
－I． 8 Subtract integers
Multiplication
－K． 1 Multiply whole numbers
－K． 3 Multiply whole numbers with four or more digits
－K． 4 Multiply numbers ending in zeroes
－K． 6 Multiply three or more numbers
－K． 8 Estimate products
－K． 9 Properties of multiplication
－K． 10 Solve for a variable using properties of multiplication
－K． 11 Integer multiplication rules
－K． 12 Multiply integers
䁲
Operations with integers
－E． 1 Integer addition and subtraction rules
－E． 2 Add and subtract integers using counters
－E． 3 Add and subtract integers
－E． 6 Integer multiplication and division rules
－E． 7 Multiply and divide integers
䉆
Operations with integers
－C． 1 Integer addition and subtraction rules
－C． 2 Add and subtract integers using counters
－C． 3 Add and subtract integers
－C． 4 Add and subtract three or more integers
－C． 6 Integer multiplication and division rules
－C． 7 Multiply and divide integers

－Job
－Addition
－Needs
皃
－Property
－Push
－Pull
篦
－Type
－Distance
－History
管
－Landforms
－Natural resources
－Tools
番
－Expansion
－Weather（ing）
霝
－Region
－View
－Model
䓵
－Technological
－Cause
署
－Impact
－Topography
篅
－Human impact
－Variation
－Angles
－Subtraction
－Tools
－Pattern
－Invent
－History
－Length
－Natural Resources
－Multiplication
－Compare
－Conclusion
－Factor
－Capacity
－Exploration
－Accuracy
－Core
－Gravity
－Solution
－Effect
－Triangle
－Speed
－Function
－Tension
－Infrastructure
－Element
－Contrast
－Parts
－Location
－Weight
－Property
－Landmark
－River
－Force
－Relationship
－Remainder
－Reconstruct
－Historian
－Prototype
－Design Constraint
－Property
－Juncture

## 

## 

- Access to videos \& links
- Cardboard
- Popsicle Sticks ( 24 for a bridge with 1 deck, 36 for 2 decks, etc.)
- String
- Scotch Tape
- Large Nail, Hobby Knife or Box cutter
- Scissors
- Ruler
- Pen/Pencil
- Sand Paper
- Elmer's Glue or Craft Glue

- Sample images of trusses \& patterns
- Craft sticks
- Glue
- Optional: Binder Clips
- Paper \& Pencils (for keeping track of budget)
- Optional: Toy train for testing

- Fact families triangles
- Whiteboard
- Whiteboard markers
- Tri-ominoes Game (chosen variation(s))
- Printouts on Cardstock
- Paper
- Pencils


## SOURCES\& REFERENCES

- http://www.instructables.com/id/Simple-Suspension-Bridge-Model/
- http://www.pbs.org/wabh/buildingbig/bridge/index.html
- http://www.pbs.org/wgbh/buildingbig/wonder/structure/akashi kaikyo.html
- https://www.youtube.com/watch?v=N9fbRcRJY34
- http://tryengineering.org/lessons/popsiclebridge.pdf

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